

60.

$$\frac{1-2\cos^2\alpha}{\sin\alpha\cos\alpha} = \operatorname{tg}\alpha - \operatorname{ctg}\alpha$$

$$\begin{aligned} \frac{1-2\cos^2\alpha}{\sin\alpha\cos\alpha} &= \frac{\sin^2\alpha + \cos^2\alpha - 2\cos^2\alpha}{\sin\alpha\cos\alpha} = \frac{\sin^2\alpha - \cos^2\alpha}{\sin\alpha\cos\alpha} \\ &= \frac{\sin^2\alpha}{\sin\alpha\cos\alpha} - \frac{\cos^2\alpha}{\sin\alpha\cos\alpha} = \frac{\sin\alpha}{\cos\alpha} - \frac{\cos\alpha}{\sin\alpha} = \operatorname{tg}\alpha - \operatorname{ctg}\alpha \end{aligned}$$

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$$\frac{\operatorname{tg}\alpha + \operatorname{tg}\beta}{\operatorname{ctg}\alpha + \operatorname{ctg}\beta} = \operatorname{tg}\alpha \cdot \operatorname{tg}\beta$$

$$\frac{\operatorname{tg}\alpha + \operatorname{tg}\beta}{\operatorname{ctg}\alpha + \operatorname{ctg}\beta} = \frac{\operatorname{tg}\alpha + \operatorname{tg}\beta}{\frac{1}{\operatorname{tg}\alpha} + \frac{1}{\operatorname{tg}\beta}} = \frac{\operatorname{tg}\alpha + \operatorname{tg}\beta}{\frac{\operatorname{tg}\beta + \operatorname{tg}\alpha}{\operatorname{tg}\alpha \cdot \operatorname{tg}\beta}} =$$

$$= \frac{\operatorname{tg}\alpha \cdot \operatorname{tg}\beta (\operatorname{tg}\alpha + \operatorname{tg}\beta)}{\operatorname{tg}\beta + \operatorname{tg}\alpha} = \operatorname{tg}\alpha \cdot \operatorname{tg}\beta$$

62.

$$(\sin\alpha + \cos\beta)^2 + (\cos\beta + \sin\alpha)(\cos\beta - \sin\alpha) = 2\cos\beta(\sin\alpha + \cos\beta)$$

$$(\sin\alpha + \cos\beta)^2 + (\cos\beta + \sin\alpha)(\cos\beta - \sin\alpha) =$$

$$= \cancel{\sin^2\alpha} + 2\sin\alpha\cos\beta + \cos^2\beta + \cos^2\beta - \cancel{\sin^2\alpha} =$$

$$= \underline{2\sin\alpha\cos\beta} + \underline{2\cos^2\beta} = 2\cos\beta(\sin\alpha + \cos\beta)$$

63.

$$(\sin\alpha - \cos\beta)^2 + (\cos\beta + \sin\alpha)(\cos\beta - \sin\alpha) = -2\cos\beta(\sin\alpha - \cos\beta)$$

$$(\sin\alpha - \cos\beta)^2 + (\cos\beta + \sin\alpha)(\cos\beta - \sin\alpha) =$$

$$= \cancel{\sin^2\alpha} - 2\sin\alpha\cos\beta + \cos^2\beta + \cos^2\beta - \cancel{\sin^2\alpha} =$$

$$= \underline{2\cos^2\beta} - \underline{2\sin\alpha\cos\beta} = 2\cos\beta(\cos\beta - \sin\alpha) = -2\cos\beta(\sin\alpha - \cos\beta)$$