

$$1.- \text{ a) } (f+g)(x) = f(x) + g(x) = \frac{2x-1}{3} + \frac{1-x}{2-x} = \frac{-2x^2+2x+5}{6-3x}$$

$$\text{ b) } (f-g)(x) = f(x) - g(x) = \frac{2x-1}{3} - \frac{1-x}{2-x} = \frac{-2x^2+8x-5}{6-3x}$$

$$\text{ c) } (f \cdot g)(x) = f(x) \cdot g(x) = \frac{2x-1}{3} \cdot \frac{1-x}{2-x} = \frac{-2x^2+3x-1}{6-3x}$$

$$\text{ d) } (f/g)(x) = f(x) : g(x) = \frac{2x-1}{3} : \frac{1-x}{2-x} = \frac{-2x^2+4x}{3-3x}$$

Dominios: $Dom f(x) = \mathcal{R}$; $Dom g(x) = \mathcal{R} - \{2\}$; a) $Dom (f+g) = \mathcal{R} - \{2\}$

b) $Dom (f-g) = \mathcal{R} - \{2\}$; c) $Dom (f \cdot g) = \mathcal{R} - \{2\}$; d) $Dom (f/g) = \mathcal{R} - \{1, 2\}$
(observa que $g(x)$ no está definida en $x = 2$, y además se anula para $x = 1$)

$$2.- \quad f(x) = \sqrt{x+1} \quad Dom f(x) = [-1, +\infty[; \quad g(x) = x+3 \quad Dom g(x) = \mathcal{R}$$

$$\text{ a) } (f+g)(x) = \sqrt{x+1} + x+3 ; \quad Dom (f+g) = [-1, +\infty[$$

$$\text{ b) } (f-g)(x) = \sqrt{x+1} - x-3 ; \quad Dom (f-g) = [-1, +\infty[$$

$$\text{ c) } (f \cdot g)(x) = (x+3)\sqrt{x+1} ; \quad Dom (f \cdot g) = [-1, +\infty[$$

$$\text{ d) } (f/g)(x) = \frac{\sqrt{x+1}}{x+3} ; \quad Dom (f/g) = [-1, +\infty[- \{3\} =]-1, 3[\cup]3, +\infty[$$

$$3.- \quad f(x) = \frac{1}{x-2} \quad Dom f(x) = \mathcal{R} - \{2\} ; \quad g(x) = \sqrt[3]{x+1} \quad Dom g(x) = \mathcal{R}$$

$$\text{ a) } (f+g)(x) = \frac{1+(x-2)\sqrt[3]{x+1}}{x-2} ; \quad Dom (f+g) = \mathcal{R} - \{2\}$$

$$\text{ b) } (f-g)(x) = \frac{1-(x-2)\sqrt[3]{x+1}}{x-2} ; \quad Dom (f-g) = \mathcal{R} - \{2\}$$

$$\text{ c) } (f \cdot g)(x) = \frac{\sqrt[3]{x+1}}{x-2} ; \quad Dom (f \cdot g) = \mathcal{R} - \{2\}$$

$$\text{ d) } (f/g)(x) = \frac{1}{(x-2)\sqrt[3]{x+1}} ; \quad Dom (f/g) = \mathcal{R} - \{-1, 2\}$$

$$4.- \text{ a) } (f \circ g)(x) = f(g(x)) = f(x^2-1) = x^2-1+2 = x^2+1$$

$$\text{ b) } (g \circ f)(x) = g(f(x)) = g(x+2) = (x+2)^2-1 = x^2+4x+3$$

$$5.- \quad \text{ a) } f \circ g = \frac{1-3x^2}{x^2}$$

$$\text{ b) } g \circ f = \frac{1}{x^2-3}$$

6.- Dadas las siguientes funciones, $f(x) = x+2$; $g(x) = \sqrt{x}$; $h(x) = x^2-2$, calcula:

$$\text{ a) } (g \circ f \circ h)(x) = g(f(h(x))) = g(f(x^2-2)) = g(x^2-2+2) = g(x^2) = \sqrt{x^2} = x$$

$$\text{ b) } f \circ g \circ h = \sqrt{x^2-2}+2 ; \quad \text{ c) } h \circ f = x^2+4x+2 ; \quad \text{ d) } g \circ h = \sqrt{x^2-2}$$